Pressure and Thrust Measurements of a High-Frequency Pulsed Detonation Tube

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This paper describes measurements of a small-scale, high-frequency pulsed detonation tube. The device utilized a mixture of H2 fuel and air, which was injected into the device at frequencies of up to 1200 Hz. Pulsed detonations were demonstrated in an 8-inch long combustion volume, at about 600 Hz, for the quarter wave mode of resonance. The primary objective of this experiment was to measure the generated thrust. A mean value of thrust was measured up to 6.0 lb, corresponding to H₂ flow based specific impulse of 2970 s. This value is comparable to measurements in H2-fueled pulsed detonation engines (PDEs). The injection and detonation frequency for this new experimental case was much higher than typical PDEs, where frequencies are usually less than 100 Hz. The compact size of the device and high frequency of detonation yields a thrust-per-unit-volume of approximately 2.0 lb/in³, and compares favorably with other experiments, which typically have thrust-per-unitvolume of order 0.01 lb/in³. This much higher volumetric efficiency results in a potentially much more practical device than the typical PDE, for a wide range of potential applications, including high-speed boundary layer separation control, for example in hypersonic engine inlets, and propulsion for small aircraft and missiles.

I. Introduction

N recent years, many studies have been conducted involving active boundary layer control techniques using pulsed combustion¹. These techniques work by manipulating the unstable free shear layer, thus exploiting the Coanda-like effect for unsteady reattachment¹. In high-speed boundary layer control applications, pulsed or synthetic jets require both high impulse and high frequency in order to be effective². Combustion-driven fluidic actuation has the potential to yield a high momentum jet by exploiting the chemical energy of the reactant fuel/air mixture¹. Because of its potential to yield high impulse at high frequencies, a pulsed detonation tube has potential as an effective flow control device. Another advantage is that it does not have many complex moving parts; therefore it should be more simple and inexpensive to manufacture.

Pulse Detonation Engines, or PDEs, are unsteady propulsion devices that use repetitive detonations to produce a periodic impulse³. The PDE differs from conventional propulsion systems in that it relies on detonation rather than deflagration of the fuel/air mixture to produce thrust.

A. Previous Work with PDEs

Several studies have been conducted for PDEs and pulsejet engines using H₂/air fuel mixtures. Early experiments conducted under J.A. Nicholls, after the end of WWII, focused on the use of intermittent detonation waves as a means of thrust⁴. In these experiments, a detonation tube was suspended using wires so that thrust would cause the tube to swing like a pendulum. Four reactant mixtures were tested: H₂/O₂, H₂/air, acetylene/O₂, and acetylene/air. When the mixture ratio was adjusted correctly, sharp, clear, and even explosions were observed at frequencies up to 35 Hz⁴. In the end, Nicholls and his team concluded that the intermittent detonation engine had many advantages, including its mechanical simplicity, static thrust capabilities, efficient operation at supersonic velocities, and potential high thrust levels or high fuel economy, but no useful applications were pursued⁴.

More recent investigations of PDEs have been conducted at the Air Force Research Laboratory using aluminum tubes, 2" ID and 36" in length⁵. Results show that average thrust increased linearly with injection frequency at approximately 0.34 lb/Hz, using stoichiometric pre-mixed H₂/air with a clean air purge fill ratio of 50%⁵. In tests with a fill fraction (i.e. the fraction of the tube filled with reactants) of 1.0 at a frequency of 16 Hz, generated thrust

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measured approximately 5.0 lb, and specific impulse was calculated to be approximately 3750 s⁵. Investigators concluded that PDE performance results are highly scalable to different injection frequencies and tube geometries. Another study conducted at AFRL was aimed at developing an enhanced combustion pulsejet engine (ECPE) for applications at Mach 0 to Mach 3⁶. Single shot detonation and cyclic detonation at 100 Hz pulsejet tube experiments were carried out using a variety of fuel-air mixtures, including H_2/O_2 , H_2/air , ethylene/air, and ethylene/ O_2 .

Investigations conducted at the General Electric Global Research Center have used ejectors to augment the thrust generated by a 2" $\rm ID \times 36$ " PDE tube burning a stoichiometric hydrogen-air fuel mixture at a frequency of $\rm 10~Hz^7$. General results show that the PDE generated a thrust of 12.9 lb, which was augmented 14% by the presence of an ejector⁷.

A separate study of a H_2 -fueled high-frequency pulse detonation engine tested a much longer PDE tube geometry, 2.95" ID \times 86.6" long. Successful tests were achieved at a maximum operating frequency of 32 Hz. In these experiments, the use of Schelkin wire (SW) was used to study its effect on lengthening or shortening the DDT distance in the PDE tube. Two SW lengths were studied, 600 mm and 1400 mm, and yielded maximum specific impulse of 1800 s and 2380 s, respectively.

B. Present Work

The present project is an extension of the work done at NASA Langley by Cutler, *et al.*, in which pulsed combustion of near-stoichiometric H_2 /air fuel was observed in chambers of varying size and geometry at various injection frequencies^{2, 9}. As in the previous experiments, time-resolved measurements of pressure at various locations in the combustion volume, pressure, temperature and rate of flow of the reactants, and injection frequency were collected. The major difference between the present test and previous tests is that thrust and specific impulse (I_{sp}) generated by the device is also measured.

II. Experimental Method

A. Pulsed Detonation Tube and High-Speed Valve

A pulsed detonation tube has been designed primarily for flow visualization experiments, although no flow visualizations are described herein. The device is actively fueled with a hydrogen-air reactant mixture through a high-frequency valve. Initially, combustion of the reactant mixture is initiated using a sparkplug. However, after the first cycle, ignition and detonation of reactants occurs by compression due to contact with reactants from the previous cycle and compression by wave propagation. Combustion products are not displaced from the combustion volume by a non-reacting gas in between each reactant injection cycle, as in typical PDEs.

Measurements of time-resolved pressure at various locations in the combustion volume, pressure, temperature and rate of flow of the reactants, and injection frequency were collected. A thrust balance was set-up in the laboratory to measure the thrust generated, and specific impulse was calculated.

Figure 1(a) is a rendering of the device, and Figure 1(b) is a photograph of the mounted assembly 10 . The combustion volume is 8" in length and has a constant rectangular cross section of 0.5" × 0.75". Windows located along the length of the combustion volume from the base of the combustion volume (x=0") to x=6" allow for flow visualization within the device, and an additional window is provided at the bottom of the device to allow a laser light sheet to pass through the plane of symmetry. In the present work, these windows were replaced with stainless steel plates. An automobile sparkplug is located at x=2.75" and is fired continuously at 120 Hz, independent of the injection frequency, ensuring that if the combustion in the tube is extinguished it is quickly reignited (conditions permitting). Pressure taps P2, P3, P4, and P4A are located at x=0.25", 4.25", 7.75", and 7.75", respectively.

The high-speed valve assembly is driven by a motor, which is in turn controlled by the data acquisition program. Figure 2 is a computer rendering of the high-speed valve assembly and rotating shaft. The valve is composed of a rotating shaft supported by high-speed bearings. The shaft rotates in a close-fitted housing with passages for air and H_2 . H_2 and air pass through the valve through a hole and a slot, respectively. The reactants are combined in a small nozzle before entering the combustion volume at a downward angle of 30° to the vertical, through a $0.335^{\circ} \times 0.335^{\circ}$ square nozzle centered at $x=5.42^{\circ}$. The shaft is turned by a high-speed motor, capable of up to about 45,000 rpm. Valve shaft position was determined using a helium-neon laser aimed at the rotating shaft through the housing assembly of the motor. The laser light is reflected off a reflective spot on the shaft onto a photodiode once per revolution.

Both H_2 and air leaked from the valve through the clearance between the valve and housing. This leakage was initially assumed to be small but was subsequently measured to be about 12% of the H_2 and 11% of the air. Flow rates quoted in this paper are nominal values, measured by the flow meters, and are not corrected for this leakage.

However, the specific impulse results are calculated using flow rates to the combustor that have been corrected.

B. Thrust Balance Set-up

In order for a small-scale, high-frequency pulsed detonation tube to be considered for the previously described applications it must be demonstrated that it provides significant thrust. A thrust balance was designed in order to measure the thrust generated by the device. Figure 3 is a simple sketch of the thrust balance used for this experiment¹⁰. The device is mounted to one end of an aluminum beam, while the other end is loaded with 70 lbs. to balance the weight of the device. The center of the beam is attached to a straight rail by means of a pair of linear ball bearings, which act as the fulcrum or pivot point for the system. Additionally, springs in tension are located on either side of the pivot point, connecting the beam to a horizontal support above, to provide a restoring force as the beam is deflected by thrust applied by the device. A linear potentiometer purchased from Celesco Transducer Products, Inc., Model CLWG-150-MC4, is attached to the system to measure displacement in response to thrust.

Calibration was conducted for the thrust balance used in these experiments. The voltage reading across the linear potentiometer needed to be converted to the proportional thrust generated by the device. In order to determine this calibration coefficient, a series of known weights were placed over the exit of the combustion volume, without the presence of any flows, at approximately one-pound increments, and then were removed in the same order. The voltage reading was recorded for each weight placed on or taken off the device. This procedure was conducted several times to ensure repeatability. Uncertainty of the balance measurement is \pm 7% due primarily to friction in the potentiometer, and the time for the balance to respond to a change is about 1sec^{10} .

C. Miscellaneous Instrumentation

Time-resolved pressure measurements were taken within the combustion chamber at P2, P3, P4, and P4A, as indicated in Figure 1(a). These measurements were taken using 0-200 psi PCB-Piezotronics pressure sensor model 113A21. Pressure taps P2 and P3 have a diameter of 0.076", and two pressure taps of different size are located at the exit, P4 and P4A. The pressure tap on the right, P4, has a diameter of 0.076", whereas the one of the left, P4A, has a larger diameter of 0.11". Simultaneous pressure data were collected to compare the time response of these two pressure taps. Preliminary runs with air only at 1704 SLPM were conducted to validate the calibration coefficients for the pressure sensors used in subsequent test runs with and without combustion.

Periodically throughout the testing period the calibration of the pressure sensors was checked, and the calibrations adjusted if required to accommodate any changes that may have occurred due to the extreme conditions to which the sensors were exposed (i.e. high heat, strong vibrations). Although calibration coefficients did change, the difference was small, no larger than 9.5% in extreme cases, but usually around $\pm 3\%^{10}$. Another problem that was encountered with the pressure sensors is that they would sometimes fail during testing. Often, the sensor in a given tap would need to be switched with a different sensor, and the case would have to be repeated. Sensor failure usually occurred at high reactant flow rates, where vibration and heat loading was the most extreme.

Simultaneous pressure data with two reactant flow rates – a low flow rate of 852 SLPM/air-341 SLPM/ H_2 and a high flow rate of 1704 SLPM/air-682 SLPM/ H_2 – at four fixed frequencies – 235, 300, 475, and 600 Hz – were collected to compare the time response of the two pressure taps located at the exit, P4 and P4A. These test runs lasted only one second, with a rate of 250,000 samples per second, to allow for better resolution of the pressure data collected. The root mean square pressure for the P4A was found to be approximately 19% (approximately 1 psi) greater than that of P4 10 . It is important to note that gauges installed in the P4A location did not fare too well in experimental runs due to high heating. If this were not the case, then all pressure taps would have been made the same size.

The spark, which is fired continuously at 120 Hz during combustion, does not have much effect on the combustion process beyond igniting combustion at the beginning of the run (or reigniting if combustion fails for some reason). Although spark firing does not have an effect on the detonation cycle, combustion appeared to have an effect on spark firing. A likely explanation for this behavior is that the combustion products have a much lower voltage threshold for arcing than the reactants or regular laboratory air. This lower voltage threshold causes arcing many times in one cycle of the spark generator when combustion products are present, which occurs at peaks in the pressure data.

Pressurized air, O_2 , and gaseous H_2 fuel were supplied to the combustor through the valve, as stated previously. Flow of H_2 was measured using a 0-1000 standard liter per minute (SLPM) Hastings mass flow meter, and flow of air was measured using a 0-2500 SLPM Hastings mass flow meter manufactured by Teledyne Hastings Instruments. In runs where O_2 -enriched air was used, flow of O_2 was measured using a 0-300 SLPM Hastings mass flow meter. Uncertainties in flow rates (after correcting for leakage) were approximately $\pm 4\%$, including uncertainty in leakage flow. Pressure taps were provided in the valve to monitor the mean pressures of the supply H_2 and air. Pressure was

measured with strain gauge type transducers with uncertainty $\pm 1\%$.

Mean pressures of the supply flows were rather high; for example, at a fuel flow rate of 1704 SLPM/air – 682 SLPM/H₂, mean pressures of the supply flows of air and hydrogen were observed at approximately 130 and 120 psi, respectively¹⁰. This high pressure is necessary to inject the reactant flow through the small orifices of the high-speed valve. The high-speed valve used in the present experiment was not developed to minimize pressure losses. In practical applications, a pulsed detonation device would have a valve optimized to minimize pressure losses (i.e., larger valve minimum areas), and, as a result, would be able to operate at lower supply pressures. However, a device such as the one presented here will always have a significant pressure drop in the injection of reactants because reactant flow is injected at a significant velocity. This is contrasted against a conventional PDE, where in principle the injection velocities are smaller, and the valve could be designed with lower pressure drops.

Figure 4 is a simple schematic of the data acquisition system as it is set up in the laboratory. On a typical run, the LabVIEW program developed for this experiment is initiated on the PC. A/D trigger settings, scope channel settings, and voltage input settings are specified to the program. Once specified reactant flow rates are established and combustion occurs, data acquisition is initiated. Data is collected for a specified amount of time (e.g., 5 seconds), after which it is downloaded to the PC. While data are being downloaded to the PC, the motor is returned to a low frequency, and any excess H₂ gas is purged from the laboratory area.

D. Data Reduction and Analysis^{2,9}

Data from the digital oscilloscope contained data points from 4 channels with 250,000 samples per channel, collected over 5 seconds: Channel 1 from the valve shaft position photodiode, Channels 2, 3, and 4 from pressure sensors at P2, P3, and P4, respectively. Signals from Channels 2, 3, and 4 were converted from voltage signals to pressure readings in psi. Data was broken into 0.1 second segments of 5000 samples per channel for reduction. A/D data from the SC-2345 contains data for 14 channels at 1000 samples per second per channel, which is broken into 0.1 second segments of 100 samples per channel.

Channel 1 photodiode data, which contains a string of pulses of finite width, was processed using Fast Fourier Transforms (FFT) to obtain valve opening frequency. Pressure data from Channels 2, 3, and 4 were analyzed to obtain two separate results. First, the short time standard deviation of pressure (RMS pressure) for each 0.1 second segment was computed. The second analysis, which required a number of steps, computed the one-cycle-delay correlation coefficient for each segment. This coefficient was obtained by shifting the data segment one reactant injection cycle and then computing the correlation between the original unshifted and the shifted segment. When the correlation coefficient is one, this indicates perfectly periodic behavior at the injection frequency, when it is zero it indicates uncorrelated behavior. Results for each segment of the data from Channels 2, 3, and 4 could be cross-plotted with the valve frequency obtained from Channel 1 data or with time into the test.

E. Test Conditions

Several types of experimental runs were conducted for the present project. The first set of runs was done to measure pressure at the three locations in the combustion volume at various reactant flow rates, scanning a number of injection frequencies for five seconds. The second set of tests consisted of 10-second runs to measure the thrust generated at various reactant flow rates and frequencies. Other types of tests included examining the role of spark firing during combustion. For these experiments, reactant flow rates studied include:

- air only (no combustion) 426, 852, 1278, and 1704 SLPM/air
- a near-stoichiometric mixture of air and H_2 426, 852, 1278, 1704, and 2130 SLPM/air with 170, 341, 511, 682, and 852 SLPM/ H_2 , respectively
- O₂-enriched air and H₂
- several fuel-lean conditions, in which air flow rate was kept constant, but H₂ flow rate was decreased.

The near-stoichiometric mixture of air and H_2 has an actual equivalence ratio of approximately 0.95. For the remainder of this discussion, tests conducted and results derived from using the near-stoichiometric mixture will be referred to as "stoichiometric".

Unless otherwise stated, results presented in this paper are derived from data collected at the reference case of $1704 \text{ SLPM/air} - 682 \text{ SLPM/} \text{ H}_2$.

III. Experimental Results

A. Pressure Time History Results

Pressure time history data were reduced to obtain RMS pressure (in psi) and one-cycle-delay correlation coefficient as a function of injection frequency. Figure 5 shows results derived from pressure time history results for experiments when combustion occurs with a near-stoichiometric fuel-air mixture at the reference flow rate. Comparison of results from cases with air only to cases with combustion shows that RMS pressure increases significantly as a result of combustion, which is to be expected.

Another effect of combustion is that the $\lambda/4$ mode resonant frequency has increased from about 400 Hz to about 600 Hz¹⁰. Resonance is identified as a frequency at which the pressure fluctuations peak and the waveform is periodic; the mode of resonance is identified by inspection of the amplitude and relative phases of waveform at the different pressure taps. The quarter wave $(\lambda/4)$ mode of resonance is where the pressure fluctuation amplitude is greatest at the closed end of the tube and zero at the exit, and the fluctuations at various pressure taps are in phase. Increase in experimentally determined resonant frequency is consistent with previous work², in which the resonant frequency was found to increase less than expected based on the higher speed of sound in the combustion products. The speed of sound in combustion products is 3200 ft/s, compared to 1130 ft/s in air. Using this new speed of sound, the theoretical resonant frequency is calculated to be 1200 Hz, which is double the experimentally obtained resonant frequency of 600 Hz. This discrepancy must be due in part to the presence of unburned reactants with lower speed of sound in the tube during much of the detonation cycle. Another cause may come from the combination of several non-linear processes occurring during detonation (i.e., formation of the shock, heat addition, combustion process, chemistry of the reactants). The present work does not include results for injection of reactants at a frequency of 1200 Hz; therefore, it cannot be said that resonance does not occur at this injection frequency. Previous work has shown that waveforms are chaotic at around 999 Hz but periodic again at about1401 Hz²; however, waveforms of these higher frequency resonances are not consistent with the $\lambda/4$ mode, but instead with another higher frequency mode, and detonations did not occur.

Figure 6 shows segments of pressure time history for the reference flow rate at two injection frequencies, about 300 Hz and 600 Hz. Valve opening, shown in red, is plotted with pressure traces collected from Channels 2, 3, and 4. During the up- and down-slope of the valve opening trace, only a fraction of the flow passages in the rotating shaft of the high-speed valve are open to the corresponding passages in the valve housing assembly. At the peak of the valve opening trace, passages are perfectly aligned, allowing for maximum injection of reactants. Figure 6 shows that detonations occur at almost every injection cycle, i.e., with each valve opening. The pressure plots for each gauge are offset vertically from each other in order to observe each individually. Therefore, only the relative values indicated on the plot are significant. The pressure amplitude is defined as the difference between minimum and peak values in a cycle.

There exists a bias error in the pressure measurements due to the small size of the pressure taps. This bias error results in the pressure amplitude of detonations being measured roughly 63% of their true value. Thus, true amplitudes of the pressure fluctuations are likely over 200 psia. The C-J prediction for detonations of stoichiometric H_2 and air at 1 atm is 168 psia². However, in reality the pressure in the combustion tube is oscillating around atmospheric pressure, and at the moment of detonation is higher than 14.7 psia. Since the C-J pressure just after detonation is expected to roughly scale with the pressure just prior to it, the pressure after detonation is expected to be greater than 168 psia. Although there are large uncertainties, it appears that the actual pressure amplitudes in the combustion tube are roughly consistent with C-J detonations.

Figure 5(b) is a plot of one-cycle-delay correlation coefficient for combustion in the detonation tube. At about 300 Hz, amplitude and shape of each pressure fluctuation are not very consistent, which is why the correlation coefficient is not very close to one. At about 600 Hz, the pressure fluctuations are more consistent from one cycle to the next, which corresponds to a local peak in the correlation coefficient. Consider Figure 6 at 600 Hz, which shows strong, periodic detonations occurring at the resonant frequency. Amplitude of the pressure fluctuation is three times that with air only (and, in reality, probably more given the bias error in the gauges). Also, detonations occur at the peak in pressure of the underlying $\lambda/4$ mode, unlike at half the resonant frequency of 300 Hz, where detonations occur just after the peak, causing a small "hump" in the waveform just before the detonation.

B. Thrust Balance Results

Thrust balance measurements were acquired at various reactant flow rates and injection frequencies. Results showed that thrust is generally a maximum at the resonant frequency, about 600 Hz, except at the highest flow rate of 2130 SLPM/air-852 SLPM/H₂. At this flow rate, maximum thrust of 6.27 lb. occurs at around 525 Hz, but it is not significantly higher (only +3.64%) than the thrust measured at approximately 600 Hz, which is 6.05 lb¹⁰.

Figure 7 is a plot of time averaged specific impulse, I_{sp} , for various frequencies at a number of near-stoichiometric reactant flow rates. At the resonant frequency of 600 Hz, the I_{sp} of the three highest flow rates is approximately 2800 s¹⁰. The close similarity between the three highest flow rates indicates that combustion is

complete at these flow rates and frequencies. At the lower flow rates, low I_{sp} is a result of incomplete combustion in the tube.

C. Miscellaneous Results

Tests were also conducted replacing 10% of the air flow with O_2 , with the flow rates otherwise kept the same as the cases with a near-stoichiometric mixture of air and H_2 . The O_2 -enriched cases were conducted to determine if combustion is complete in the device, and to determine if the performance is limited by reaction rate. In the near-stoichiometric case, there is exactly enough O_2 present in the air to completely consume the H_2 , assuming that H_2 and air mix perfectly; however, the addition of O_2 to the airflow may help the H_2 to be consumed more completely in cases where H_2 and air do not mix perfectly. Results with O_2 -enriched air and H_2 were compared to the near-stoichiometric cases. If H_2 and air mix perfectly, and all the H_2 reacts, then the cases with added O_2 should yield the same heat release, thrust, and RMS pressure. Increase in RMS pressure in cases with added O_2 would indicate that the O_2 -enriched mixture are small, then it can be assumed that the reaction of O_2 is complete without the additional O_2 . Another effect of O_2 addition is to increase the rate of reaction.

At lower flow rates, introduction of O_2 into the reactant mixture increased RMS pressure fluctuations from gauge P2 by about 40% at lower injection frequencies and about 25% at higher injection frequencies. Similarly, P3 RMS pressure fluctuations increased approximately 20% at lower injection frequencies, but no significant changes are noticed at high frequencies or in P4 RMS pressure fluctuations 10 . This increase in RMS pressure reaffirms the fact that reaction was not complete at this low flow rate without the addition of O_2 . For the higher flow rate, the addition of O_2 in the reactant mixture does not significantly change the RMS pressure for any of the gauges. This indicates that mixing and combustion of the reactant mixture was complete without the addition of O_2 . Also, RMS pressure fluctuations for the O_2 -enriched cases appear to peak at similar injection frequencies as the normal combustion cases, indicating that there is no change in the resonant frequency when O_2 is introduced into the reactant mixture.

Two fuel-lean cases were chosen for continued testing to compare to a case with a near-stoichiometric mixture of air and H_2 at the highest flow rate (2130 SLPM/air – 852 SLPM/ H_2). Detonations continued to occur at the resonant frequency of around 600 Hz; however, this injection frequency did not yield maximum thrust or I_{sp} , as it did in the near-stoichiometric cases. Figure 8 is a plot of the I_{sp} calculated from steady-state thrust at various injection frequencies for three reactant flow rates: a near-stoichiometric reactant mixture of air and H_2 at the highest flow rate and two fuel-lean mixtures of 2130 SLPM/air-739 SLPM/ H_2 (fuel lean case 1) and 2130 SLPM/air-682 SLPM/ H_2 (fuel lean case 2). Thrust generated at the fuel-lean conditions ranged between 4.5 and 6.0 lb. A maximum I_{sp} of 3400 s was calculated for fuel lean case 2 at an injection frequency of about 425 Hz^{10} .

Specific impulse differs greatly at the lower injection frequencies, which is a result of the inconsistent behavior of the thrust generated. However, at around 600 Hz, the I_{sp} of the two fuel-lean cases shown is approximately 2700 s, which is similar to the three highest near-stoichiometric flow rates plotted in Figure 7^{10} . The explanation for this trend is not known. It is possible that there are two offsetting trends whose effect depends on frequency. On the one hand, a fuel-lean condition tends to reduce the reactivity of the reactants, which would be expected to reduce I_{sp} . On the other hand, fuel-lean increases the mass of the reactants per unit mass of fuel (H_2), similar to reducing the fill fraction, which in PDEs increases I_{sp} . Further studies will need to be conducted in order to clearly understand the effects of operating fuel-lean.

D. Discussion and Comparison to Literature

Table 1 summarizes the results of thrust balance tests presented. Maximum thrust and I_{sp} are tabulated for each reactant flow rate along with corresponding injection frequency at which the maximum occurs. The last column in Table 1 is the percent difference in I_{sp} for each case, using the reference flow rate at around 600 Hz as the point of comparison. This result was chosen to be the reference I_{sp} because it was the case with a near-stoichiometric reactant mixture that produced the best results.

Table 1 Summary of performance at 600 Hz injection frequency with various reactant flow rates 10.

The low I_{sp} value at the two lowest reactant flow rates yield a large percent difference to the reference case. This

Nominal flow rate of Air, SLPM	Nominal flow rate of H ₂ , SLPM	Injection frequency, Hz	Thrust, lb	I _{sp} , s	Difference in I _{sp} , %
426	170	750	0.39	900	-70%
852	341	750	1.8	2100	-29%
1278	511	600	3.7	2800	-5.7%
1704	682	600	5.2	2970	
2130	852	525	6.3	2900	-2.4%
2130	682	425	5.9	3400	14%
2130	738	300	5.6	2900	-2.4%

attributed to incomplete combustion at these low flow rates. At the higher near-stoichiometric flow rates, the percent difference is much smaller. The maximum I_{sp} for the fuel lean case 1 had no significant difference from the reference case, whereas maximum I_{sp} for fuel lean case 2 had a larger difference of $14\%^{10}$.

It is useful to compare the thrust balance and I_{sp} results from this experiment to those of H₂-fueled PDEs from other research facilities. Table 2 lists the results from such experiments. Although the detonation tube discussed here did not produce the largest specific impulse compared to the PDE work, it has larger I_{sp} than those of many of the references. Also, the device is much smaller in size than the comparable PDEs. When normalized by combustion tube volume, the detonation tube presented here is far superior to the PDEs considered. The compact size results in a low weight-to-thrust ratio, which is desirable in aircraft and missile applications. It is also important to note that the device presented here operated at much higher injection frequencies than those in the other experiments listed.

Table 2 Summary of results for various experiments¹⁰.

Reference	Frequency, Hz	Volume, V in ³	Fill Fraction	Thrust, T	Isp, s	T/V, lb/in ³
Nicholls ⁴	26.7	226	<1	3.2	2100	0.0141
AFRL (a) ⁵	16	452	1	6.7	3750	0.0147
AFRL (b) ⁵	16	452	0.3	3.7	7100	0.0083
GE-GRC ⁷	10	485	1	12.9	1070	0.0266
Zhang ⁸	32	2370	N/A		~2000	
Present Work ¹⁰	600	3	1.71*	5.18	2970	1.73

For the results shown in Table 2 for the present experiment, combustion tube fill fraction is reported as 1.71 for at the reference flow rate at 600 Hz injection frequency. This value is based on the assumption that the combustion tube pressure is 1 atm (14.7 psia), and implies that some of the reactants are "spilling" out of the tube during operation¹⁰. Given that the pressure within the tube when it is filled with reactants is higher than atmospheric, it is likely that the reactants do not in fact significantly spill from the tube.

IV.Conclusions

Experiments have been conducted to investigate a pulsed detonation tube 10 . The combustion volume was 8" in length and had a rectangular cross-section of 0.5" \times 0.75". A near-stoichiometric mixture of H_2 and air was supplied to the tube at various flow rates and at frequencies of up to 1000 Hz. Thrust balance measurements were conducted to determine the thrust and I_{sp} generated by the device at different operating conditions.

The major contribution of the present work, as opposed to previous work², is that a thrust balance system was developed and used in order to determine the thrust generated during operation. As expected, detonations in a near-stoichiometric mixture of H_2 /air were accomplished in the short λ /4 resonant tube, specifically at high reactant flow rates at around 600 Hz and 300 Hz. Addition of O_2 into the reactant mixture helped enhance combustion at lower reactant flow rates. At higher flow rates, mixing and combustion of H_2 and air was already complete; therefore, the addition of O_2 did not change the behavior of the device.

Maximum thrust attained was approximately 6.0 lbf at the highest reactant flow rate of 2130 SLPM/air-852

SLPM/ H_2 at the resonant frequency, about 600 Hz^{10} . As expected, thrust increased with reactant flow rate. Specific impulse was consistent for the three highest reactant flow rates at the resonant frequency, with less than a 6% difference from the reference value of 2970 s at a nominal flow rate of 1704 SLPM/air-682 SLPM/ H_2^{10} . At the lower flow rates, detonations did not occur at each injection cycle and combustion was not complete, causing low thrust and I_{sp} .

Fuel-lean conditions were also tested to determine the effect on thrust. Two fuel-lean cases were tested to compare to a case with a near-stoichiometric mixture of air and H_2 at the highest flow rate. Detonations continued to occur at the resonant frequency of around 600 Hz; however, this injection frequency did not yield maximum thrust or I_{sp} , as it did in the stoichiometric cases. Thrust generated at the fuel-lean conditions ranged between 4.5 and 6.0 lb. A maximum I_{sp} of 3400 s was calculated for a reactant mixture of 2130 SLPM/air-682 SLPM/ H_2 at an injection frequency of around 425 Hz^{10} . It is speculated that there are two offsetting trends whose relative importance depends on frequency. First, the reactivity of the reactants would be reduced in fuel-lean cases, and so I_{sp} would be expected to decrease. However, fuel-lean conditions are known to increase I_{sp} . Further studies will need to be conducted in order to clearly understand the effects of operating with fuel-lean conditions.

As stated previously, the combustion volume for this device has a rectangular cross-section, which enables the device to be fitted with windows. Internal flow visualization of the combustion volume was not conducted in the present work, but images of the combustion volume during detonation cycles will lead to a better understanding of the gas dynamics occurring within the device. In future work, flow visualization of the combustion volume and exhaust jet should be conducted. Also, higher frequencies of operation, up to 1400 Hz, should be tested to observe the thrust of the device at higher injection frequencies. As in past studies^{2,9}, operation at around 1400 Hz, which corresponds to the $3\lambda/4$ waveform, resulted in perfectly periodic deflagration combustion at each injection cycle. This behavior may also be observed in the device if further tests were conducted.

This device was developed primarily as an actuator for flow control. The high specific impulse and high frequencies of operation give it much promise in high-speed boundary layer separation control applications, for example in hypersonic engine inlets. However, possible applications are not limited to flow control. Other applications of a high-frequency PDE include small-scale propulsion applications—such as high-speed munitions, small missiles, supersonic reconnaissance vehicles, and pressure-rise combustors for gas turbine engines. Because of this potential, future research on these applications is encouraged.

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